## New Results for Fuzzy Generalized Continuous Functions

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#### Abstract

In this paper, a new class of functions called fuzzy continuous function, fuzzy generalized continuous function and fuzzy  $\delta g$ -irresolute mappings has been defined and its properties are investigated. Examples and counter examples are given.

Keywords and phrases: Fuzzy  $\delta$ -continuity, fuzzy  $\delta$ -generalized continuity, fuzzy  $\delta$ g-irresolute mappings, fuzzy topological space, fuzzy generalized closed set, fuzzy  $\delta$ -generalized closed set, fuzzy continuous function, fuzzy generalized continuous function, fuzzy  $\delta$ g-irresolute mappings.

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#### **1. INTRODUCTION**

Zadeh [6] introduced the fundamental concept of fuzzy sets. The concept of fuzzy topological spaces was introduced in [5]. The concept of extension of fuzzy topological spaces introduced by [2]. And the generalized fuzzy continuous functions was introduced by [3].

Let  $(X, \tau)$  be a fuzzy topological space and  $\tau \subset \tau *$  then  $\tau *$  will be called a simple extension of  $\tau[2]$  if there exists of  $\delta \notin \tau$  such that

 $\tau^* = \{\lambda \lor (\mu \land \delta) / \lambda, \, \mu \in \tau\}$ 

In this case, we write  $\tau^* = \tau$  ( $\delta$ ). In this paper, we introduce a new definitions of fuzzy  $\delta$ - continuous function, fuzzy  $\delta$ - closed set, fuzzy  $\delta$ g- continuous functions. Throughout this paper X and Y represents the fuzzy topological spaces (X,  $\tau$ ) and (Y,  $\sigma$ ).

#### 2. PRELIMINARIES

A fuzzy topology  $\tau$  [5] on X is a collection of subsets of  $\tau$  such that

- (i) 0,  $1 \in \tau$  (or  $0_x, 1_x \in \tau$ )
- (ii) If  $\lambda$ ,  $\mu \in \tau$  then  $\lambda \lor \mu \in \tau$
- (iii) $\lambda_i \in \tau$  for each  $i \in \tau$  then  $\forall \lambda_i \in \tau$

The ordered pair  $(X, \tau)$  is called a fuzzy topological space (in short fts) and members of  $\tau$  are called  $\tau$ -fuzzy open sets or simply fuzzy open sets.

A fuzzy set  $\lambda$  in a fuzzy topological space is called a fuzzy closed set if its complement (1- $\lambda$ ) is fuzzy open set. Cl ( $\lambda$ ) denotes the closure of  $\lambda$  and is given by

Cl ( $\lambda$ ) =  $\wedge$  { $\mu/\mu$  is fuzzy closed and  $\mu \ge \lambda$  }.

Int ( $\lambda$ ) denotes the interior of  $\lambda$  and is given by

Int  $(\lambda) = \lor \{ \mu/\mu \text{ is fuzzy open and } \mu \leq \lambda \}$ 

#### **Definition: 2.1**

A fuzzy set  $\lambda$  in a fts (X,  $\tau$ ) is called

- (i) fuzzy semi open [1] if  $\lambda \leq Cl$  (Int ( $\lambda$ )).
- (ii) fuzzy pre open [4] if  $\lambda \leq \text{Int}(\text{Cl}(\lambda))$ .
- (iii) fuzzy  $\alpha$  open [4] if  $\lambda \leq \text{Int} (\text{Cl}(\text{Int}(\lambda)))$ .
- (iv) fuzzy generalized closed (Briefly,fg-closed) [1] if  $Cl(\lambda) \le \mu$  whenever  $\lambda \le \mu$ and  $\mu$  is fuzzy open in  $(X, \tau)$ .

#### **Definition: 2.2**

A mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is said to be

- (i) fuzzy continuous [5] if  $f^{-1}(\lambda)$  is fuzzy open set in  $(X, \tau)$ , for each fuzzy open set  $\lambda$  in  $(Y, \sigma)$ .
- (ii) fuzzy pre Continuous [4] if  $f^{-1}(\lambda)$  is fuzzy pre open set in  $(X, \tau)$ , for each fuzzy open set  $\lambda$  in  $(Y, \sigma)$ .
- (iii) fuzzy  $\alpha$ -continuous [4] if  $f^{-1}(\lambda)$  is fuzzy  $\alpha$ -open set in  $(X, \tau)$ , for each fuzzy open set  $\lambda$  in  $(Y, \sigma)$ .
- (iv) fuzzy g-continuous [3] if  $f^{-1}(\lambda)$  is fg-closed set in  $(X, \tau)$ , for each fuzzy closed set  $\lambda$  in  $(Y, \sigma)$ .

### 3. NEW FORMS OF FUZZY CONTINUITY BY SUITABLE CHOICE OF $\boldsymbol{\delta}$

#### **Definition: 3.1**

Let  $f : (X, \tau) \to (Y, \sigma)$  and  $\delta$  be a non fuzzy open set of  $(X, \tau)$  then f is called a fuzzy  $\delta$ - continuous function, if  $f^{-1}(\lambda)$  is an fuzzy open set in  $(X, \tau^*)$  for every fuzzy open set  $\lambda$  in  $(Y, \sigma)$ .

#### **Preposition: 3.1**

Let  $f:(X, \tau) \to (Y, \sigma)$  be a fuzzy continuous function and let  $\delta$  be a non-fuzzy open subset in  $(Y, \sigma)$  if  $f^{-1}(\delta)$  is a fuzzy open set of  $(X, \tau)$  then  $f : (X, \tau) \to (Y, \sigma^*)$  is a fuzzy continuous function.

#### **Proof:**

Let  $f : (X, \tau) \to (Y, \sigma)$  be a fuzzy continuous function and  $\delta \notin \sigma$  be a non fuzzy open subset in  $(Y, \sigma)$  and let  $\sigma \subset \sigma^*$ . Let  $\beta$  be a fuzzy open set in  $(Y, \sigma^*)$  Then  $\beta = \lambda \lor (\mu \land \delta)$  where  $\lambda$  and  $\mu$  are fuzzy open sets in  $(Y, \sigma)$ .

$$\begin{split} f^{1}(\beta) &= f^{1}(\lambda \lor (\mu \land \delta)) \\ &= f^{1}(\lambda) \lor (f^{1}(\mu) \land f^{1}(\delta)) \end{split}$$

Since f is a fuzzy continuous function and assumption that  $f^{-1}(\delta)$  is a fuzzy open set of  $(X, \tau)$  then  $f^{-1}(\beta)$  is fuzzy open subset of  $(X, \tau)$  which implies that

f:  $(X, \tau) \rightarrow (Y, \sigma^*)$  is a fuzzy continuous function.

#### **Preposition: 3.2**

Let  $f : (X, \tau) \to (Y, \sigma)$  be a fuzzy continuous function and  $\delta \notin \tau$  be a non fuzzy set in  $(X, \tau)$  then  $f : (X, \tau^*) \to (Y, \sigma)$  is a fuzzy continuous function.

#### **Proof:**

Let  $f : (X, \tau) \to (Y, \sigma)$  be a fuzzy continuous function and  $\delta \notin \tau$  be a non fuzzy open subset in  $(X, \tau)$ . Let  $\tau \subset \tau^*$  and Consider  $f : (X, \tau^*) \to (Y, \sigma)$ . Then this function f is fuzzy continuous function, since every fuzzy open set in  $(X, \tau)$  is an fuzzy open set in  $(X, \tau^*)$  and since  $f : (X, \tau) \to (Y, \sigma)$  is a fuzzy continuous functions.

#### **Preposition: 3.3**

Let  $f : (X, \tau) \to (Y, \sigma)$  be a fuzzy continuous function and  $\delta_1$  be a non fuzzy open subset in  $(X, \tau)$  and  $\delta_2$  be a non fuzzy open subset in  $(Y, \sigma)$ , if  $f^{-1}(\delta_2)$  is a fuzzy open set in  $(X, \tau (\delta_1))$ , then f:  $(X, \tau (\delta_1)) \to (Y, \sigma (\delta_2))$  is a fuzzy continuous function.

#### Proof

Let  $f: (X, \tau) \to (Y, \sigma)$  be a fuzzy continuous function and  $\delta \notin \tau$  be a non–fuzzy open set in  $(X, \tau)$  and let  $\tau \subset \tau^*$ . Consider  $f: (X, \tau(\delta_1)) \to (Y, \sigma)$  since every fuzzy open set in  $(X, \tau)$  is an fuzzy open set in  $(X, \tau(\delta_1))$  and since  $f: (X, \tau) \to (Y, \sigma)$  is a fuzzy continuous function. Then  $f: (X, \tau(\delta_1)) \to (Y, \sigma)$  is a fuzzy continuous function.

Let  $\delta_2 \notin \sigma$  be a non fuzzy open subset in  $(Y, \sigma)$  Let  $\sigma \subset \sigma^*$ , where  $\sigma^*$  be a simple extension of  $\sigma$  if and only if there exist  $\delta_2 \notin \sigma$  such that  $\sigma^* = \{\lambda \lor (\mu \land \delta) / \lambda, \mu \in \sigma\}$ . In this case, we write  $\sigma^* = \sigma(\delta_2)$ . Let  $\beta$  be an fuzzy open set in  $(Y, \sigma(\delta_2))$ , then  $\beta = \lambda \lor (\mu \land \delta_2)$  where  $\lambda$  and  $\mu$  are fuzzy open set in  $(Y, \sigma)$ 

$$\begin{split} f^{1}\left(\beta\right) &= f^{1}(\lambda \lor (\mu \land \delta_{2})) \\ &= f^{1}(\lambda) \lor (f^{1}(\mu) \land f^{1}(\delta_{2})) \end{split}$$

Since f is a fuzzy continuous function and the assumption that  $f^{-1}(\delta_2)$  is an fuzzy open set in  $(X, \tau(\delta_1)), f^{-1}(\beta)$  is a in fuzzy open set in  $(X, \tau(\delta_1))$  then  $f: (X, \tau(\delta_1)) \rightarrow (Y, \sigma((\delta_2)))$  is a fuzzy continuous function.

#### **Preposition : 3.4**

Every fuzzy continuous function is a fuzzy  $\delta$ - continuous function.

#### **Proof:**

Let  $f: (X, \tau) \to (Y, \sigma)$  is a fuzzy continuous function then  $f^{-1}(\lambda)$  is a fuzzy open set in  $(X, \tau)$  for every fuzzy open set  $\lambda$  in  $(Y, \sigma)$ . Let us consider  $\delta \notin \tau$  be a non fuzzy open subset in  $(X, \tau)$ , then consider  $\tau \subset \tau^*$ . Consider  $f:(X, \tau^*) \to (Y, \sigma)$  is a fuzzy continuous function. Since  $f: (X, \tau) \to (Y, \sigma)$  is a fuzzy continuous function and every fuzzy open set in  $(X, \tau)$  is a fuzzy open set in  $(X, \tau^*)$ , then  $f^{-1}(\lambda)$  is an fuzzy open set in  $(X, \tau^*)$ .

Hence  $f: (X, \tau^*) \rightarrow (Y, \sigma)$  is a fuzzy  $\delta$ - continuous function.

#### Remark :3.1

The converse of preposition 3.2 is not always true as shown by the following example.

#### Example :3.1

Let X = {a, b, c},  $\tau = \{1, 0, \lambda\}$  where  $\lambda: X \to [0, 1]$  is defined by  $\lambda(a) = 0$ ,  $\lambda(b) = 0$ ,  $\lambda(c) = 1$ . Then (X,  $\tau$ ) is a fuzzy topological space. Let  $\delta$  be a non fuzzy open set in (X,  $\tau$ ) where  $\delta: X \to [0,1]$  is defined by  $\delta(a) = 0$ ,  $\delta(b) = 1$ ,  $\delta(c) = 0$  then  $\tau(\delta) = \{0, 1, \lambda, \delta, \lambda \lor \delta\}$  be the fuzzy topology on X and let Y= {a,b,c},  $\sigma = \{1, 0, \lambda\}$  is the fuzzy topology on Y, where  $\lambda(a) = 0$ ,  $\lambda(b) = 0$ ,  $\lambda(c) = 1$ .

If  $f: (X, \tau) \to (Y, \sigma)$  defined by f(a) = a, f(b) = c, f(c) = b then  $f^{-1}(\lambda) = \delta$  since  $\delta$  is a fuzzy open set in  $(X, \tau^*)$ . Then f is a fuzzy  $\delta$ -continuous function, but not a fuzzy continuous function.

# 4. NEW FORMS OF FUZZY GENERALIZED CONTINUITY BY SUITABLE CHOICE OF $\boldsymbol{\delta}$

#### **Definition: 4.1**

A fuzzy subset  $\lambda$  of a space  $(X, \tau)$  is said to be fuzzy  $\delta$ - generalized closed set (Briefly, fuzzy  $\delta$ g-closed) if  $\delta$ Cl $(\lambda) \leq \beta$  whenever  $\lambda \leq \beta$  and  $\beta$  is fuzzy open in  $(X, \tau)$  where  $\delta$ Cl $(\lambda)$  is given by  $\delta$ Cl $(\lambda) = \wedge \{\gamma \leq 1 : \lambda \leq \gamma, \text{ whenever } \gamma \text{ is a fuzzy closed set } \tau^* \}$ .

A fuzzy subset of X belonging to  $\tau^*$  is denoted by fuzzy  $\delta$ - open set, the complement of fuzzy  $\delta$ -open set is denoted by fuzzy  $\delta$ - closed set .

The family of all fuzzy  $\delta$ - open set is denoted by  $F\delta O(X)$  and the family of all  $\delta$ -fuzzy closed sets is denoted by  $F\delta C(X)$ .

#### **Definition: 4.2**

A function  $f : (X, \tau) \to (Y, \sigma)$  is called a fuzzy  $\delta$ -continuous function if  $f^{-1}(\lambda)$  is a  $\delta$ -fuzzy closed set in  $(X, \tau)$ , for every closed set  $\lambda$  in  $(Y, \sigma)$ .

#### **Definition: 4.3**

A function  $f : (X, \tau) \to (Y, \sigma)$  is called  $\delta g$ -fuzzy continuous function. if  $f^{-1}(\lambda)$  is a fuzzy  $\delta g$ - closed set in  $(X, \tau)$ , for every closed set  $\lambda$  in  $(Y, \sigma)$ .

#### **Preposition : 4.4**

For a fuzzy subset of a space  $(X, \tau)$  and a function  $f : (X, \tau) \to (Y, \sigma)$  from the definition stated above, we have the following diagram of implications.

fuzzy continuous function	$(3) \rightarrow$	g-fuzzy continuous function
(1)↓		$\downarrow$ (4)

fuzzy  $\delta$ -continuous function (2) $\rightarrow$  fuzzy  $\delta$ g- continuous function

#### Proof

- Since f is a fuzzy continuous function then f<sup>-1</sup>(λ) is a fuzzy open set in (X, τ) for every fuzzy open set λ in (Y, σ) but every fuzzy open set in (X, τ) is a fuzzy open set in (X, τ\*) => f<sup>-1</sup>(λ) is a fuzzy δ- open set in (X, τ\*) for every fuzzy open set λ in (Y, σ) => f is a fuzzy δ-continuous function.
- 2) Since f is a δ-fuzzy continuous function then f<sup>-1</sup>(λ) is a fuzzy δ-closed set in (X, τ) for every fuzzy closed set λ in (Y, σ). But every fuzzy δ- closed set in (X, τ) is a fuzzy δg-closed set in (X, τ)=> f<sup>-1</sup>(λ) is a fuzzy δg- closed set in (X, τ) for every fuzzy closed set λ in (Y, σ) => f is a fuzzy δg-continuous function.
- 3) Since f is a fuzzy continuous function then  $f^{-1}(\lambda)$  is a fuzzy closed set in  $(X,\tau)$  for every fuzzy closed set  $\lambda$  in  $(Y,\sigma)$  But every fuzzy closed set in  $(X,\tau)$  is a g-fuzzy closed set in  $(X,\tau)$  then  $f^{-1}(\lambda)$  is a g-fuzzy closed set in  $(X, \tau)$  for every fuzzy closed set  $\lambda$  in  $(Y, \sigma) => f$  is a g-fuzzy continuous function.
- 4) Since f is g-fuzzy continuous function then f<sup>-1</sup>(λ) is a g-fuzzy closed set in (X,τ) is a fuzzy δ-closed set in (X,τ\*) => every fuzzy δ-closed set is a δg-fuzzy closed set => f<sup>-1</sup>(λ) is a δg-fuzzy closed set in (X, τ\*) for every fuzzy

closed set  $\lambda$  in (Y,  $\sigma$ ) => f is a fuzzy  $\delta$ g- continuous function.

#### Example: 4.6

Let X = Y = {a, b, c} Define fuzzy sets  $\lambda$ ,  $\delta$ ,  $\beta$ : X = Y  $\rightarrow$  [0, 1] by the equation  $\lambda(a) = 0.5$ ,  $\lambda(b) = 0$ ,  $\lambda(c) = 0$   $\delta(a) = 0$ ,  $\delta(b) = 0.6$ ,  $\delta(c) = 0$ , and  $\beta(a) = 0.6$ ,  $\beta(b) = 0.6$ ,  $\beta(c) = 1$  then

 $\tau = \{1, 0, \lambda, \beta\}$  is a fuzzy topology on X and  $\sigma = \{1, 0, \delta\}$  is a fuzzy topology on Y. Let  $\delta$  be the non fuzzy open set in  $(X, \tau)$  then  $\tau (\delta) = \{1, 0, \lambda, \delta, \lambda \lor \delta\}$ . Let  $\lambda_1(a) = 0.4$ ,  $\lambda_1(b) = 0$ ,  $\lambda_1(c) = 0$  be the fuzzy subset in  $(X, \tau)$ . If  $f : (X, \tau) \to (Y, \sigma)$  defined by,

- a) f(a) = a, f(b) = b and f(c) = c then f is a fuzzy  $\delta$ -continuous function but not a fuzzy continuous function.
- b) f (a) = f (c) = b, and f (b) = a then f is a fuzzy g-continuous function but not a fuzzy continuous function.

#### 5. ON FUZZY δg-CONTINUOUS FUNCTION

#### **Definition: 5.1**

A mapping  $f:(X,\tau)\to(Y,\sigma)$  is said to be fuzzy  $\delta$ -irresolute (briefly,  $f\delta$ -irresolute) if  $f^{-1}(\lambda)$  fuzzy  $\delta$ -closed set in X, for every closed set  $\lambda$  in Y.

#### **Definition : 5.2**

A mapping  $f:(X,\tau)\to(Y,\sigma)$  is said to be fuzzy  $\delta$ -generalized irresolute (briefly, f $\delta$ g-irresolute) if  $f^{-1}(\lambda)$  is f $\delta$ g-closed set in X, for every  $\delta$ g-closed set  $\lambda$  in Y.

#### Theorem : 5.1

Every  $f\delta g$ -irresolute mapping is  $f\delta g$ -continuous.

#### **Proof:**

Let  $f : (X, \tau) \to (Y, \sigma)$  is fog-irresolute. Let  $\lambda$  be a fuzzy closed set in Y. Then  $\lambda$  is fog-closed fuzzy set in Y. Since f is fog-irresolute.  $f^{-1}(\lambda)$  is fog-closed set in X. Hence f is fog-continuous.

#### Remark : 5.1

However the converse of the above theorem need not be true as seen from the following example.

#### Example : 5.1

Let  $X = Y = \{a, b, c\}$ . Define fuzzy sets  $\lambda$ ,  $\delta_1$ ,  $\delta_2 : X \rightarrow [0, 1]$  by the equation ,  $\lambda (a) = 0.5$ ,  $\lambda (b) = 0$ ,  $\lambda (c) = 1$ ,

 $\delta_1(a) = 0,$   $\delta_1(b) = 0.6,$   $\delta_1(c) = 0,$  $\delta_2(a) = 0,$   $\delta_2(b) = 0,$   $\delta_2(c) = 0.7$ 

and  $\gamma : Y \rightarrow [0, 1]$  defined by  $\gamma(a) = 1$ ,  $\gamma(b) = 0.5$ ,  $\gamma(c) = 0$ .

 $\tau = \{1, 0, \lambda\}$  is a fuzzy topology on  $(X, \tau)$ .  $\sigma = \{1, 0, \gamma\}$  is a fuzzy topology on  $(Y, \sigma)$ . Let  $\delta_1$  be the non fuzzy open set in  $(X, \tau)$ , then  $\tau(\delta_1) = \{1, 0, \lambda, \delta_1, \lambda \lor \delta_1\}$  and  $\delta_2$  be the non fuzzy open set in  $(Y,\sigma)$ , then  $\sigma(\delta_2)=\{1, 0, \gamma, \delta_2, \gamma \lor \delta_2\}$ . Let  $f : (X, \tau) \rightarrow (Y, \sigma)$  defined by f(a) = b, f(b) = a, f(c) = c, then f is fuzzy  $\delta g$ -continuous function. But f is not f $\delta g$ -irresolute.

#### **Definition:5.3**

A mapping  $f : (X, \tau) \to (Y, \sigma)$  is said to be fuzzy  $\delta$ -closed mappings if  $f(\lambda)$  is fuzzy  $\delta$ -closed in  $(Y, \sigma)$ , for every fuzzy closed set  $\lambda$  in X.

#### **Definition:5.4**

A mappings  $f : (X, \tau) \to (Y, \sigma)$  is said to be fuzzy  $\delta g$ -closed mappings if  $f(\lambda)$  is fuzzy  $\delta g$ -closed in  $(Y, \sigma)$ , for every fuzzy closed set  $\lambda$  in X.

#### **Definition:5.5**

If every fuzzy  $\delta g$ -closed in X is f $\delta$ -closed in X, then the space can be denoted as  $f\delta T_{1/2}$ -space.

#### Theorem:5.2

A fuzzy topological space (X,  $\tau$ ) is  $f\delta T_{1/2}$ -space if and only if  $F\delta O(X, \tau) = FG\delta O(X, \tau)$ .

#### **Proof:**(Necessity)

Let  $(X, \tau)$  be  $f\delta T_{1/2}$ -space.Let  $\lambda \in FG\delta O(X, \tau)$ , then  $1-\lambda$  is a fog-closed set.Thus  $\lambda \in F\delta O(X, \tau)$ . Hence  $F\delta O(X, \tau) = FG\delta O(X, \tau)$ .

#### (sufficiency)

Let  $F\delta O(X, \tau) = FG\delta O(X, \tau)$ . Let  $\lambda$  is a f $\delta$ g-closed.Then 1- $\lambda$  is a f $\delta$ g-open.Hence 1- $\lambda \in F\delta O(X, \tau)$ .Thus  $\lambda$  is a f $\delta$ -closed set.Therefore  $(X, \tau)$  is a f $\delta T_{1/2}$ -space.

#### Theorem:5.3

Let  $f: (X, \tau) \to (Y, \sigma)$  be fog-continuous. Then f is fuzzy  $\delta$ -continuous if  $(X, \tau)$  is  $f\delta T_{1/2}$ -space.

#### **Proof:**

Let  $\lambda$  be a fuzzy closed of  $(Y, \sigma)$ . Since f is f $\delta$ g-continuous, f<sup>-1</sup>( $\lambda$ ) is f $\delta$ g-closed set of  $(X, \tau)$ . Again  $(X, \tau)$  is a f $\delta$ T<sub>1/2</sub>-space and hence f<sup>-1</sup>( $\lambda$ ) is a f $\delta$ -closed set of  $(X, \tau)$ . This implies that f is fuzzy  $\delta$ -continuous.

#### Example:5.2

Let  $X = Y = \{a, b, c\}$ . Define fuzzy sets  $\lambda, \delta : X \rightarrow [0, 1]$  by the equation ,

 $\lambda$  (a) = 0.5,  $\lambda$  (b) = 0,  $\lambda$  (c) = 1,

 $\delta(a) = 0, \ \delta(b) = 0.6, \ \delta(c) = 0,$ 

and  $\gamma : Y \rightarrow [0, 1]$  defined by  $\gamma(a) = 1$ ,  $\gamma(b) = 0.5$ ,  $\gamma(c) = 1$ .

 $\tau = \{1, 0, \lambda\}$  is a fuzzy topology on  $(X, \tau)$ .  $\sigma = \{1, 0, \gamma\}$  is a fuzzy topology on  $(Y, \sigma)$ . Let  $\delta$  be the non fuzzy open set in  $(X, \tau)$ , then  $\tau (\delta) = \{1, 0, \lambda, \delta, \lambda \lor \delta\}$ . Let  $f : (X, \tau) \to (Y, \sigma)$  defined by f (a) = b, f (b) = a, f (c) = c, then f is fuzzy  $\delta g$ -continuous function. But  $\lambda$  is not  $f \delta T_{1/2}$ -space as  $\lambda$  is not  $f \delta$ -closed set of  $(X, \tau)$ . Then f is not fuzzy  $\delta$ -continuous.

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